

9. cvičení

a) IS pro $\hat{\beta}_i$: $T_i = \frac{\hat{\beta}_i}{\sqrt{\hat{\sigma}^2 (\mathbf{X}^T \mathbf{X})^{-1}_{ii}}} \sim t(n-p)$

Pak $P(\left|T_i\right| < \left|\frac{\hat{\beta}_i}{\sqrt{\hat{\sigma}^2 (\mathbf{X}^T \mathbf{X})^{-1}_{ii}}}\right|) = 1 - \alpha$
 $\left|\frac{\hat{\beta}_i}{\sqrt{\hat{\sigma}^2 (\mathbf{X}^T \mathbf{X})^{-1}_{ii}}}\right| \leq \frac{\hat{\beta}_i}{\sqrt{\hat{\sigma}^2 (\mathbf{X}^T \mathbf{X})^{-1}_{ii}}} \leq \frac{\left|\hat{\beta}_i\right|}{\sqrt{\hat{\sigma}^2 (\mathbf{X}^T \mathbf{X})^{-1}_{ii}}}$
Z čehož dostaneme $\left|\hat{\beta}_i\right| \sim t(1 - \frac{\alpha}{2}, n-p)$

b) $T = \frac{\mathbf{a}^T \mathbf{b}}{\sqrt{\mathbf{a}^T \mathbf{X}^T \mathbf{X} \mathbf{a}}} \sim t(n-p)$

$\left|T\right| \sim t(1 - \frac{\alpha}{2}, n-p)$

A regresní přímka pro dívky bude mít tvar $y = \hat{\beta}_0 + \hat{\beta}_1 x$. Pro chlapce: $y = \hat{\beta}_0 + \hat{\beta}_1 + (\hat{\beta}_1 + \hat{\beta}_3)x$. IS pro $\hat{\beta}_1 + \hat{\beta}_3$, tedy $\mathbf{a} = (0, 1, 0, 1)$

d) Při počítání predikčního intervalu zohledňujeme chybu u "nového pozorování". Tedy odhad rozptylu je $\hat{\sigma}^2 \mathbf{x}^T (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{x} + \hat{\sigma}^2$.
 $\text{implies } T = \frac{\mathbf{x}^T \mathbf{b}}{\sqrt{\hat{\sigma}^2 (1 + \mathbf{x}^T (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{x})}} \sim t(n-p)$

```
# Confidence interval  
predict(..., interval = "confidence")  
  
# Or  
predict(..., interval = "prediction")
```

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